## ST EDWARD'S

## OXFORD



# 13+ SCHOLARSHIP EXAMINATION 2010 

## MATHEMATICS <br> PAPER I

1 hour

Answer all questions.
Calculators are permitted.
$\qquad$

1. Lisa used $\frac{1}{2}$ of her lottery win to buy a house.

She gave $\frac{1}{6}$ of her lottery win to a charity.
Lisa then shared the remainder of her lottery win equally between her four children. Work out the fraction of Lisa's lottery win that each of her four children received.
2. (a) Simplify
(i) $3 a+4 b-2 a-b$
(ii) $5 x^{2}+2 x-3 x^{2}-x$
(b) Expand the brackets
(i) $4(2 x-3)$
(ii) $p\left(q-p^{2}\right)$
(c) Expand and simplify $5(3 p+2)-2(5 p-3)$
3. The fraction, $p$, of an adult's dose of medicine which should be given to a child who weighs $w$ kg is given by the formula

$$
p=\frac{3 w+20}{200}
$$

A child weighs 35 kg .
(a) Work out the fraction of an adult's dose which should be given to this child. Give you answer as a fraction in its simplest form.
(b) Use the formula $p=\frac{3 w+20}{200}$ to find the weight of a child whose dose is the same as an adult's dose.
4. (a) Solve $7 p+2=5 p+8$

$$
\begin{equation*}
p=. \tag{2}
\end{equation*}
$$

(b) Solve $7 r+2=5(r-4)$

$$
r=\text {.......................... }
$$

5. The first term of a sequence is 7 .

The rule for the sequence is Add 5 to the previous term.
(a) Write down the second term and the third term of the sequence.
(b) Work out the 10th term of the sequence.
$\qquad$
(c) Write down an expression, in terms of $n$, for the $n$th term of the sequence.
6. 20 students took a short test.

The table gives information about their marks in the test.

| Mark | Frequency |  |
| :---: | :---: | :---: |
| 7 | 1 |  |
| 8 | 5 |  |
| 9 | 7 |  |
| 10 | 9 |  |

Work out the mean mark.
7. 80 students each study one of three languages.

The two-way table shows some information about these students.

|  | French | German | Spanish | Total |
| :---: | :---: | :---: | :---: | :---: |
| Female | 15 |  |  | 39 |
| Male |  | 17 |  | 41 |
| Total | 31 | 28 |  | 80 |

(a) Complete the two-way table.

One of these students is to be picked at random.
(b) Write down the probability that the student picked studies French.
(Total 3 marks)
8.


Diagram NOT accurately drawn

Calculate the size of the exterior angle of a regular hexagon.
9. Solve

$$
\frac{x}{3}-5=3(x-2)
$$

$$
x=
$$

(Total 4 marks)
10. (a) (i) Solve the inequality

$$
5 x-7<2 x-1
$$

(ii) On the number line, represent the solution set to part (i).

$n$ is an integer such that $-4 \leq 2 n<3$.
(b) Write down the possible values of $n$.
11.


Diagram NOT accurately drawn

The diagram shows a cylinder with a height of 10 cm and a radius of 4 cm .
(a) Calculate the volume of the cylinder.

Give your answer correct to 3 significant figures.

The length of a pencil is 13 cm .
The pencil cannot be broken.
(b) Show that this pencil cannot fit inside the cylinder.
12.


Diagram NOT
accurately drawn

The diagram shows a sector of a circle, centre $O$.
The radius of the circle is 9 cm .
The angle at the centre of the circle is $40^{\circ}$.
Find the perimeter of the sector.
Leave your answer in terms of $\pi$.
13.


Diagram NOT accurately drawn

Cylinder A and cylinder B are mathematically similar.
The length of cylinder $\mathbf{A}$ is 4 cm and the length of cylinder $\mathbf{B}$ is 6 cm .
The volume of cylinder $\mathbf{A}$ is $80 \mathrm{~cm}^{3}$.
Calculate the volume of cylinder B.
14. Solve the simultaneous equations

$$
\begin{aligned}
& 3 x-4 y=11 \\
& 5 x+6 y=12
\end{aligned}
$$

$$
\begin{aligned}
& x= \\
& y=
\end{aligned}
$$

